

NOMOGRAPHY FOR OPERATIONS RESEARCH

Russell C. Coile

Professional Paper No. 187

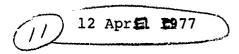
April 1977

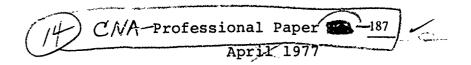


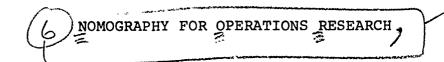
The ideas expressed in this paper are those of the author. The paper does not necessarily represent the views of either the Center for Naval Analyses or the Department of Defense.

> CENTER FOR NAVAL ANALYSES 1401 Wilson Boulevard

Arlington, Virginia 22209







Russell C./Coile

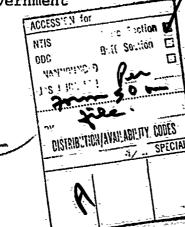
Center for Naval Analyses University of Rochester

Paper to be presented at the Joint National Meeting of the Operations Research Society of America and The Institute for Management Services

San Francisco, California

9 May 1977

The views expressed in this paper are those of the author and do not reflect those of the U.S. Navy, the Department of Defense, or any other Government agency.



47727p Done

NOMOGRAPHY FOR OPERATIONS RESEARCH

ABSTRACT

Nomographs have been found to be useful in operations research. These charts for graphical computation have the advantages to the user of being non-electronic, quick, and easy to use. They can be designed to present complicated mathematical formulas in a simple format to non-mathematical people. Disadvantages are the slide-rule type accuracy and the possible lack of feel that families of curves might possibly give.

Research on applications of nomographs in solving operations research problems has lead to development of some procedures for simplified design of nomographs. Examples of nomographs for acoustical design, radar, and sonar illustrate these procedures.

Figure

NOMOGRAPHY FOR OPERATIONS RESEARCH

Russell C. Coile

Center for Naval Analyses

INTRODUCTION

Nomographs are charts for graphical calculations. Nomography Figure 2 was invented by a French engineer, Maurice d'Ocagne, in 1884. He coined the word "nomography" from the Greek nomos, law, and the Greek graphos, drawn or written, to describe these graphical representations of mathematical laws. Nomographs are also called nomograms or alignment charts.

Nomographs have a number of advantages over other methods of computation in some operations research situations. They are non-figure

3 electronic, quick and easy to use. They do not require interpolation. The designer of the nomograph can pre-digest the mathematics and make the graphical computation palatable for non-mathematical people. Also, some problems permit a translation of variables into more familiar terms. The disadvantages of nomographs are the lack of accuracy and the lack of "feel" that some graphical displays of curves might give.

The approach I will use this morning is to show you how easy

it is to construct nomographs for operations research applications.

First we will examine the classification of equations into the types that are appropriate for nomography. Then we will use a worksheet for planning the scale equations and scale spacing. Finally,

we will use plotting charts to mark the scales. Then I will show you some examples of nomography. As a matter of fact, may I show you one example right now? Suppose you were concerned with doppler shift in underwater acoustics as a function of relative velocity and sonar frequency. The nomograph for Doppler Shift has three scales; Δf , doppler shift in Hertz, v, relative velocity in knots, and f sonar frequency in kiloHertz. The nomograph is a graphical representation of the formula

$$\Delta f = \frac{2v}{c} f$$

where c is the velocity of sound.

To use the nomograph, one can lay a straight-edge between 5 knots on the relative velocity scale and 20 kiloHertz on the sonar frequency scale and read the answer of 70 Hertz on the Δf doppler shift scale.

CONSTRUCTION OF NOMOGRAPHS

The first step in nomography is examination of the mathematical formula. Nomographs can usually be constructed for equations of three variables which are or can be manipulated into the form called Type I below.

Type I equations.

$$\tilde{f}_{1}(x) + \tilde{f}_{2}(y) = \tilde{f}_{3}(z)$$

Nomographs can similarly be constructed for equations of four or more variables of the Type II form.

Type II equations,

Figure

$$f_1(x) + f_2(y) + f_3(z) = f_4(r)$$

Figures
8&9 equation for each line after we have decided on the general approach
and the spacing between lines. A nomograph Work Smeet helps organize
these calculations. An example has been worked out for a military
problem of estimating the possible radius of an enemy submarine's
escape circle after loss of contact by an anti-submarine ship. In
this example,

Figures

vt = r

where

v submarine speed in knots

t elapsed time in hours

r radius of sub escape circle in nautical miles

Some nomographic plotting charts developed at M.I.T.'s Mathe
matical Laboratory in 1918 by Professor Joseph Lipka (Reference 1)

Figures
12&13 will be found to be useful in marking the scales. Both uniform and logarithmic scales can be easily marked using these MIT charts.

NOMOGRAPHIC ACCURACY

Nomographs have slide-rule type accuracy. Nomographs constructed in the original French style originated by d'Ocagne have poorer accuracy as the number of variables increases. However, Professor Brodetsky (Reference 2) of Leeds University in England Figures 14-22

developed a method for preserving accuracy no matter how many variables are involved. For example, a nomograph for the multiplication of (X) and (Y) in the French style results in the product answer (XY) on the inside being at half-scale. The English method would put the answer on the outside at full scale. Similarly, the multiplication of (X), (Y) and (Z) in the French style ends up with the (XY)Z answer on the inside at one-quarter scale. The English method preserves full scale accuracy for the answer on the outside. Division is handled in a similar fashion.

An example of seven variables illustrates how powerful this English method is. Professor Brodetsky also suggested starting with the evaluation of the denominator first in the sequence of calculations. Hence in the design of a nomograph for

Figure 23

$$A = \frac{XYZ}{PQR}$$

what we actually do is consider this to be

$$A = \left(\left[\frac{X}{(PQ)R} \right] Y \right) Z$$

and begin with PxQ, then (PQ) x R, etc.

LOGARITHMIC VX LINEAR SCALES

Some nomographs may be easier to use if made with linear rather than logarithmic scales. The nomograph for

Figures 24&25

$$z = \frac{yQ}{2}$$

can be designed for either logarithmic or linear scales as illustrated.

EXAMPLES

A nomograph which could be used in search and rescue operations for planning the number of aircraft required to search an ocean area for an aircraft forced down at sea is based on the following expression given by Morse and Kimball (Reference 3)

Figure 26

$$p = 1 - e^{-\left(\frac{WLN}{A}\right)}$$

where

p the percent chance of detection

W sweep width in miles

L length of search track

N number of search aircraft

A area to be searched in square miles

The target strength of fish as a function of size (length, actually) and sonar frequency is based on the following expressions developed by Love (Reference 4)

Figure

$$T_{D} = 19.1 \log L + 0.9 \log \lambda - 34.2$$

$$T_S = 22.8 \log L - 2.8 \log \lambda - 32.4$$

where

Tn target strength in dB for dorsal aspect

 $\mathbf{T}_{\mathbf{S}}$ target strength for side aspect

L length of fish in feet,

\(\lambda \) wavelength of sound in feet.

Figure

28 percent has been designed to assist in determining when enough is enough. Various states have different levels of blood-alcohol concentration for legal definitions of intoxication. I believe the official BAC level in California is 0.1%. If you weigh 140 pounds or fewer, it would not appear to be prudent (or legal) to drink more than two Manhattans within an hour at the ORSA mixer tonight if you plan to drive shortly thereafter.

REFERENCES

- Lipka, Joseph. <u>Graphical and Mechnical Computation</u>. Wiley,
 New York, 1918
- Brodetsky, S. <u>A First Course in Nomography</u>. G. Bell and Sons,
 Ltd., London 1920
- 3. Morse, Philip M. and Kimball, George E. Methods of Operations
 Research. Wiley, New York, 1951
- Love, Richard H. "Maximum Side-Aspect Target Strength of an Individual Fish" Journal of the Acoustical Society of America, Vol. 46, No. 3 (Part 2) pages 746-752, 1969

NOMOGRAPHY

FOR

OPERATIONS RESEARCH

BY

RUSSELL C. COILE

"NOMOGRAPH"

GREEK NOMOS LAW

GREEK GRAPHOS DRAWN OR

WRITTEN

GRAPHICAL REPRESENTATION OF A MATHEMATICAL LAW

ALSO CALLED "NOMOGRAM"

NOMOGRAPHS

ADVANTAGES TO CONSUMER

No Electronics
Quick
Easy to Use
No Interpolation
Predigested Math
Translated Variables

DISADVANTAGES

Accuracy
No "Feel"

APPROACH

CLASSIFICATION OF EQUATIONS

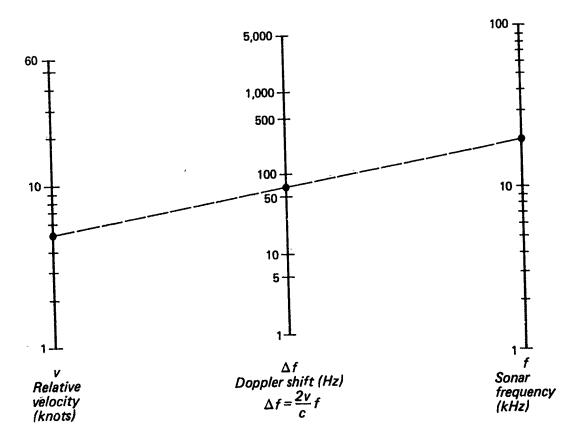
WORKSHEET

Scale Equations

Scale Spacing

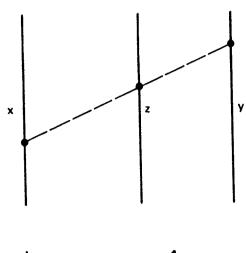
PLOTTING CHARTS

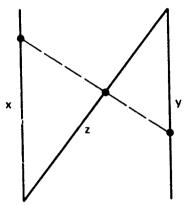
EXAMPLES



PRINCIPLES OF UNDERWATER SOUND R.J. Urick, McGraw Hill, 1975, Page 294.

FIG. 5: DOPPLER SHIFT





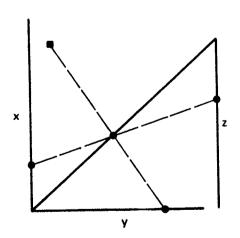


FIG. 6: TYPES OF EQUATIONS i. $f_1(x) + f_2(y) = f_3(z)$

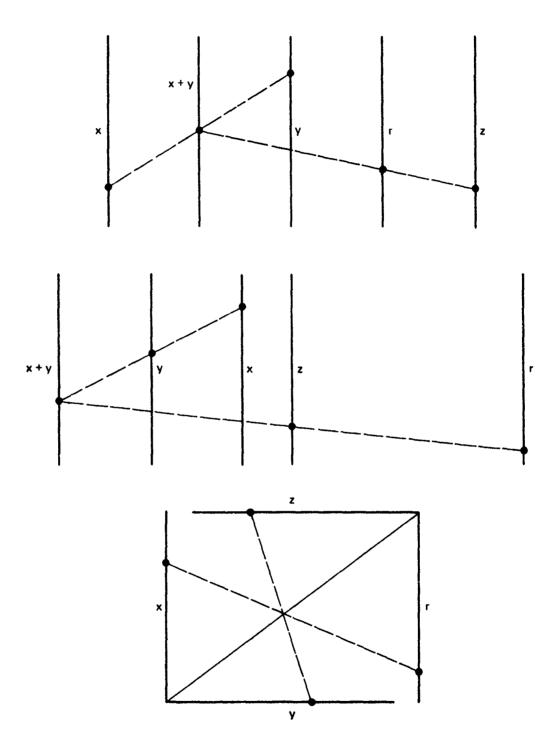


FIG. 7: TYPES OF EQUATIONS II. $f_1(x) + f_2(y) + f_3(z) = f_4(r)$

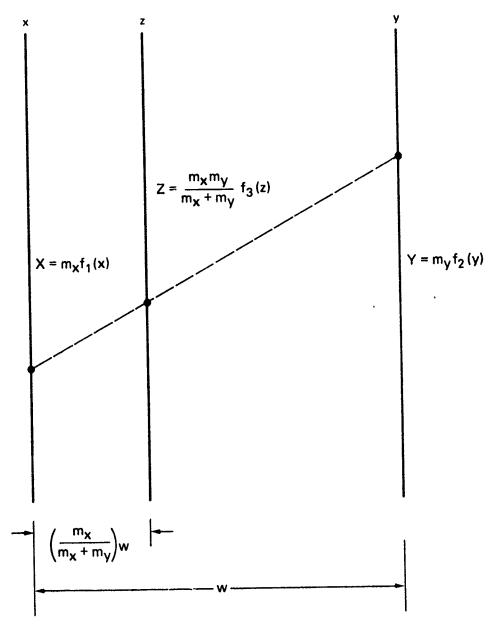
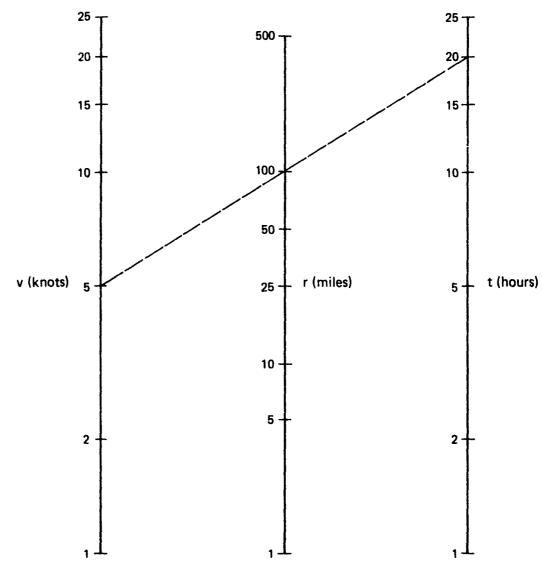


FIG. 8: TYPES OF EQUATIONS i. $f_1(x) + f_2(y) = f_3(z)$

NOMOGRAPH	WORK	SHEET
MOMOGIVAETI	MOWN	THEFT

Step	NOMOGRAPH WORK SHEET						
I	Identify the	type of t	he equation	1.			
II	Scale X]	Range	Trial factor length/range	Scale Factor	Plotting Equation	
111	Scale Y	1	Range	Trial factor length/range	Scale Factor	Plotting Equation Y	
ΊV	Scale Z		e factor x ^m y +m y		m _z	z	
v	Z spącing fro	$m X = \left(\frac{m}{x}\right)^{\frac{1}{2}}$	w (w				
VI	Z starting points						
VII	Draw X scale				***************************************		
WII	Draw Y scale						
IX	Draw Z scale						
х	Check the Nomograph Nomograph						
ХI	Complete the 1. Title 2. Equation		3. Scales	labeled with sy	rmbols a	nd units	

· I	Identify the type of the equation. $v + t = v$ $f_1(x) + f_2(y) = f_3(3)$ in Type T $log v + log t = log v$
II	Scale $X = M_X \log V$ Range $log 25 = 1.4$ $-log 1 = 0$ 1.4 Trial factor Scale Plotting length/range Factor Equation $\frac{6}{1.4} = 4.3$ $\frac{1}{1.4} \times 1.4$ $\frac{1}{1.4} \times 1.4$
III	Scale Range Plotting length/range Factor Equation
IV	Scale Scale factor $z = m \int_{z}^{m} \int_{x+m}^{m} \int_{y-4}^{x+m} \int_{y-4}^{$
V	Z spacing from $X = \left(\frac{m_X}{m_X + m_Y}\right) w = \left(\frac{4}{4 + 4}\right) 4 = 2$ (NCHES
VI	$1(10) = 10$ 2 starting points $25(2) = 50$ $\sqrt{t} = 1$ $5(10) = 50$
VII	Draw X scale of V IN KNOTS
MII	Draw Y scale of A IN HOURS
IX	Draw Z scale OF / IN MILES
	Check the Nomograph Nomograph
X .	
ХI	Complete the Nomograph 1. Title 3. Scales labeled with symbols and units 2. Equation 4. Sample index line



vt = r

- v Sub speed in knots t Elapsed time in hours r Radius of sub escape circle in miles

FIG. 11: RADIUS OF SUBMARINE ESCAPE CIRCLE AFTER LOSS OF ASW CONTACT

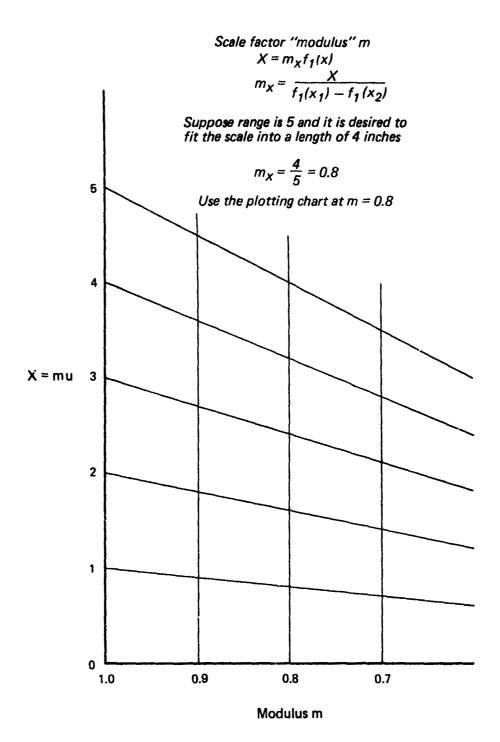


FIG. 12: SCALES FOR NOMOGRAPHS

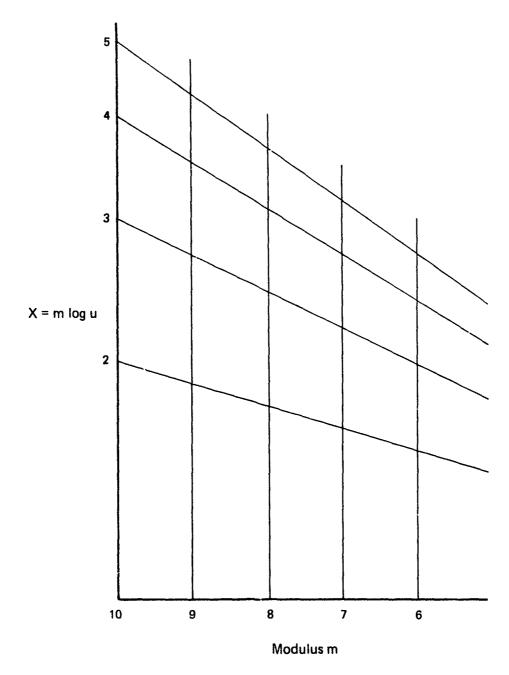


FIG. 13: LOGARITHMIC SCALES

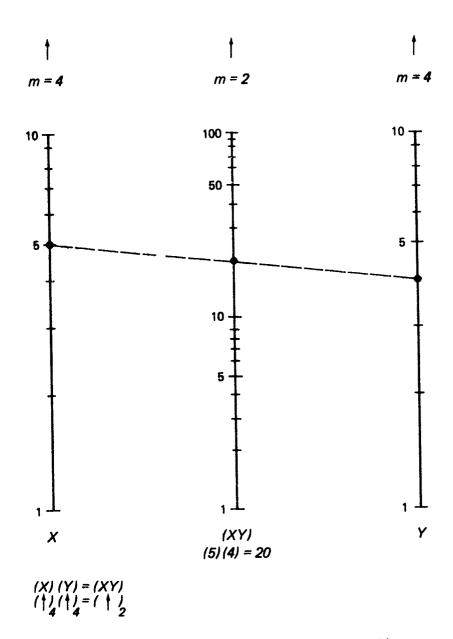


FIG. 14: MULTIPLICATION (ANSWER: INSIDE)

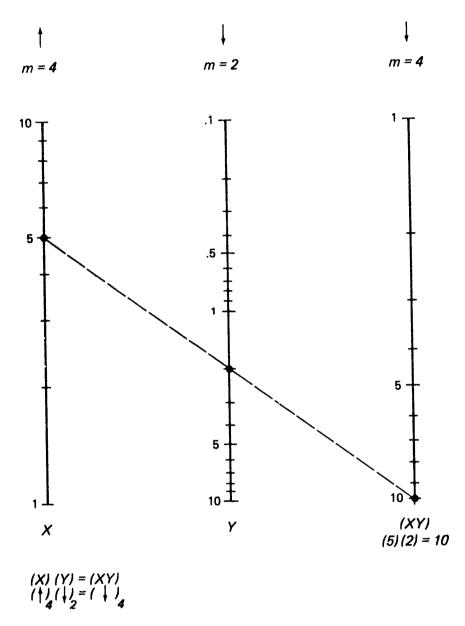


FIG. 15: MULTIPLICATION (ANSWER:OUTSIDE)

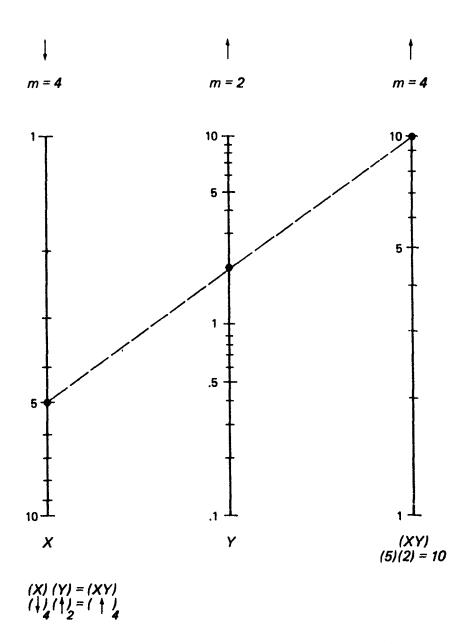


FIG. 16: MULTIPLICATION (ANSWER:OUTSIDE)

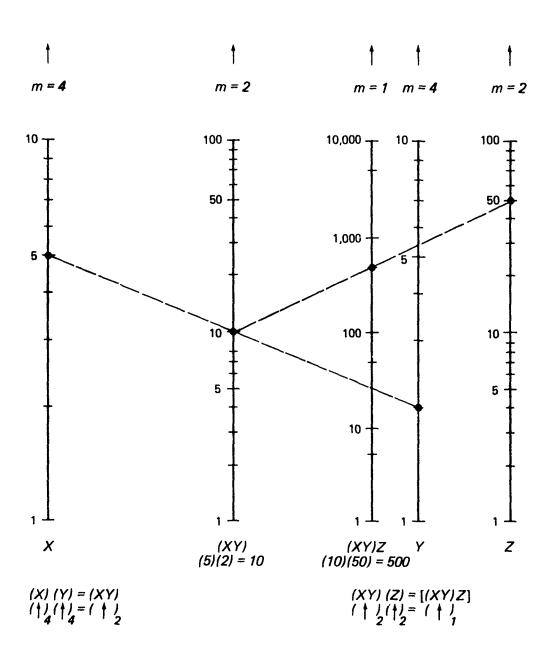


FIG. 17: MULTIPLICATION (ANSWER: INSIDE)

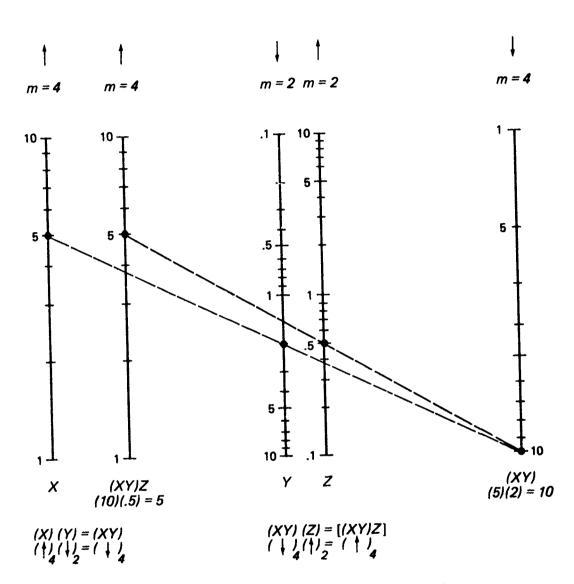
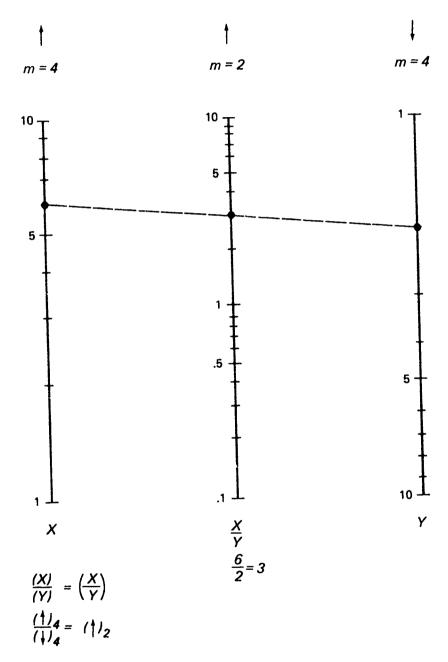


FIG. 18: MULTIPLICATION (ANSWER:OUTSIDE)



TO THE WASHINGTON TO THE PROPERTY OF THE PROPE

FIG. 19: DIVISION (ANSWER: INSIDE)

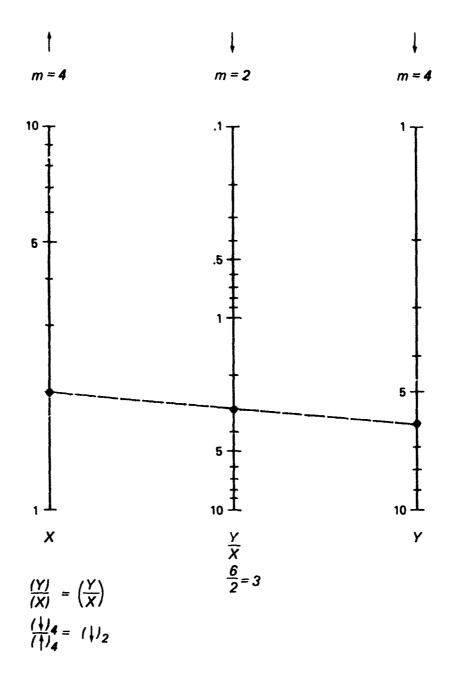


FIG. 20: DIVISION (ANSWER: INSIDE)

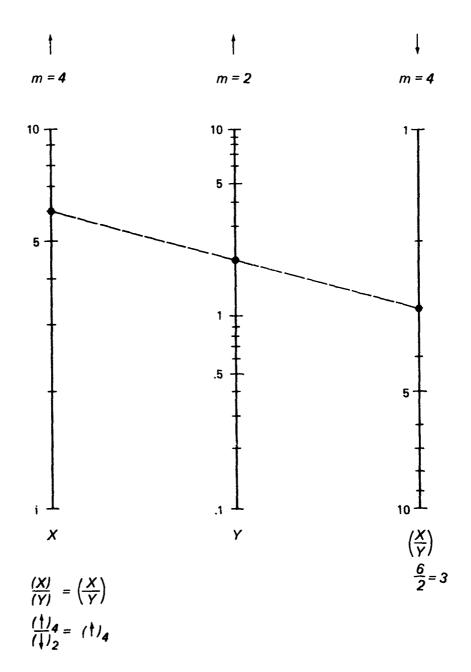


FIG. 21: DIVISION (ANSWER:OUTSIDE)

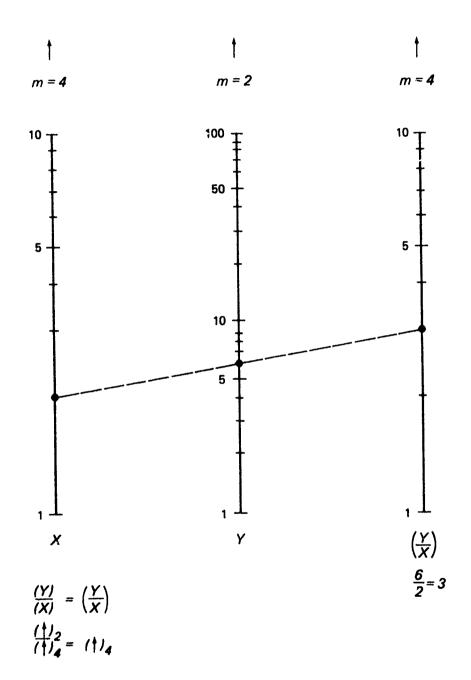
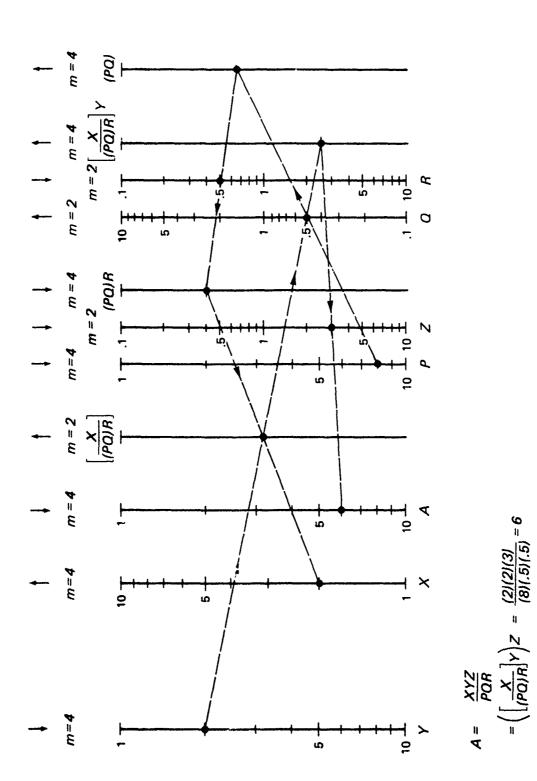
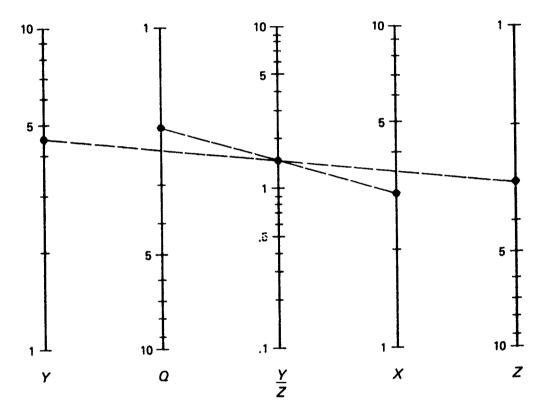


FIG. 22: DIVISION (ANSWER: OUTSIDE)

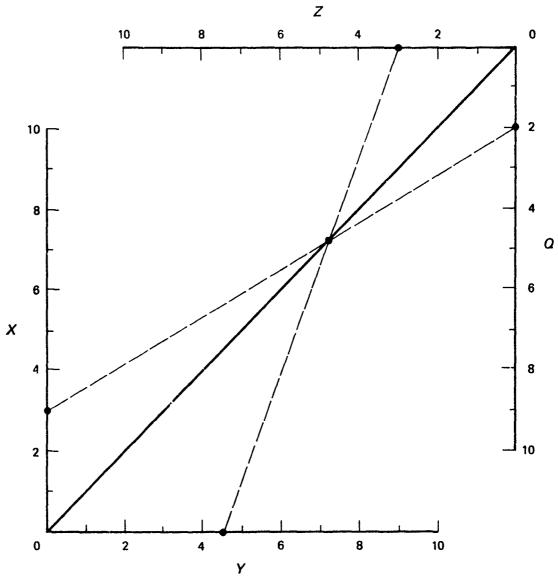






$$X = \frac{YQ}{Z} = \frac{(4.5)(2)}{3} = 3$$

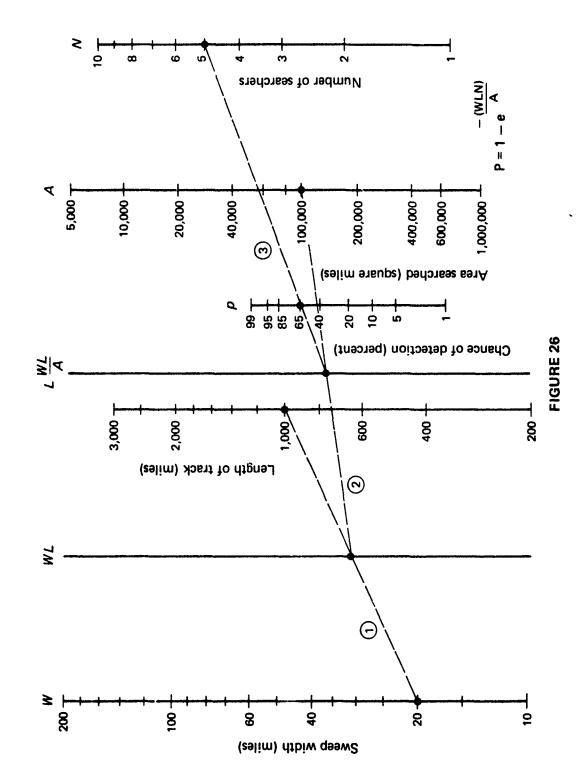
FIGURE 24



$$X = \frac{YQ}{Z} = \frac{(4.5)(2)}{3} = 3$$

Note: $\frac{m_X}{m_Y} \frac{m_Q}{m_Z}$

FIGURE 25



The transfer of the first of the second state of the second secon

TARGET STRENGTHS OF AN INDIVIDUAL FISH*

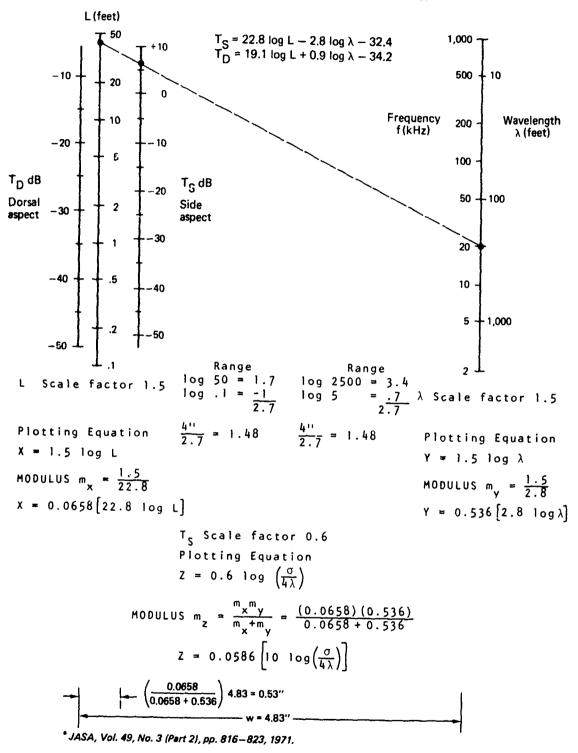


FIGURE 27

BAR-O-GRAPH BAC (BLOOD-ALCOHOL CONCENTRATION) (PERCENT)

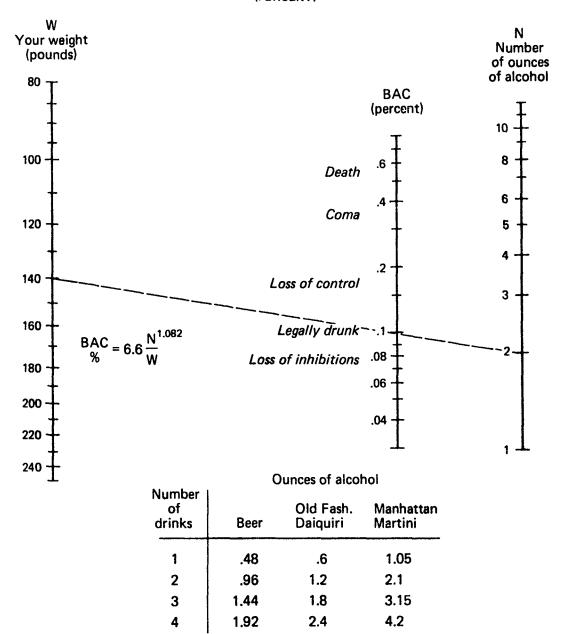


FIGURE 28

CNA Professional Papers — 1973 to Present*

PP 103

矿

Friedheim, Robert L., "Political Aspects of Ocean Ecology" 48 pp., Feb 1973, published in Who Protects the Oceans, John Lawrence Hargrove (ed.) (St. Paul. West Publig Co., 1974), published by the American Society of International Law) AD 757 936

PP 104

Schick, Jack M., "A Review of James Cable, Gunboat Diplomacy Political Applications of Limited Naval Forces," 5 pp., Feb 1973, (Reviewed in the American Political Science Review, Vol. LXVI, Dec 1972)

Corn, Robert J and Phillips, Gary R, "On Optimal Correction of Gunfire Errors," 22 pp, Mar 1973, AD 761 674

Stoloff, Peter H., "User's Guide for Generalized Factor Analysis Program (FACTAN)," 35 pp , Feb 1973, (Includes an addendum published Aug 1974) AD 758 824

Stoloff, Peter H., "Relating Factor Analytically Derived Measures to Exogenous Variables," 17 pp., Mar 1973, AD 758 820

PP 108

McConnell, James M and Kelly, Anne M, "Super-power Naval Diplomacy in the Indo-Pakistani Crisis," 14 pp., 5 Feb 1973, (Published, with revisions, in Surrival, Nov/Dec 1973) AD 761 675

Berghoefer, Fred G., "Salaries-A Framework for the Study of Trend," 8 pp., Dec 1973, (Published in Review of Income and Wealth, Series 18, No 4, Dec

PP 110

Augusta, Joseph, "A Critique of Cost Analysis," 9 pp., Jul 1973, AD 766 376

Herrick, Robert W, "The USSR's 'Blue Belt of Defense' Concept. A Unified Military Plan for Defense Against Seaborne Nuclear Attack by Strike Carriers and Polaris/Poseidon SSBNs," 18 pp., May 1973, AD 766 375

PP 112

Ginsberg, Lawrence H, "ELF Atmosphere Noise Level Statistics for Project SANGUINE," 29 pp , Apr 1974, AD 786 969

Ginsberg, Lawrence H, "Propagation Anomalies During Project SANGUINE Experiments," 5 pp , Apr 1974, AD 786 968

Maloney, Arthur P., "Job Satisfaction and Job Turnover," 41 pp., Jul 1973, AD 768 410

The section of the se

Silverman, Lester P., "The Determinants of Emergency and Elective Admissions to Hospitals," 145 pp., 18 Jul 1973, AD 766 377

Rehm, Allan S., "An Assessment of Military Opera itions Research in the USSR," 19 pp. Sep 1973, (Reprinted from Proceedings, 30th Military Opera-tions Research Symposium (U), Secret Dec 1972)

PP 117

McWhite, Peter B and Ratliff, H Donald, "Defending a Logistics System Under Mining Attack," ** 24 pp., Aug 1976 (to be submitted for publication in Naval Research Logistics Quarterly), presented at 44th National Meeting, Operations Research Society of America, November 1973, AD A030 454 *University of Florida

**Research supported in part under Office of Naval Research Contract N00014-68-0273-0017

Barfoot, C. Bernard, "Markov Duels," 18 pp., Apr 1973, (Reprinted from Operations Research, Vol. 22, No 2, Mar-Apr 1974)

PP 119

Stoloff, Peter and Lockman, Robert F, "Development of Navy Human Relations Questionnaire," 2 pp, May 1974, (Published in American Psychological Association Proceedings, 81st Annual Convention, 1973) AD 779 240

PP 120

Smith, Michael W and Schrimper, Ronald A.,

"Economic Analysis of the Intracity Dispersion of
Criminal Activity," 30 pp., Jun 1974, (Presented at
the Econometric Society Meetings, 30 Dec 1973)
AD 780 538

*Economics, North Carolina State University.

PP 121

Devine, Eugene J., "Procurement and Retention of Navy Physicians," 21 pp., Jun 1974, (Presented at the 49th Annual Conference, Western Economic Association, Las Vegas, Nev., 10 Jun 1974) AD 780 539

Kelly, Anne M, "The Soviet Naval Presence During the Iraq-Kuwaiti Border Dispute: March-April 1973," 34 pp., Jun 1974, (Published in Soviet Naval Policy, ed. Michael MccGwire; New York. Praeger) AD 780 592

Petersen, Charles C., "The Soviet Port-Clearing Operation in Bangladash, March 1972-December 1973," 35 pp., Jun 1974, (Published in Michael MccGwire, et al. (eds) Soviet Naval Policy: Objectives and Constraints, (New York: Praeger Publishers, 1974) AD 780 540

Priedheim, Robert L. and Jehn, Mary E, "Anticipating Soviet Behavior at the Third U.N. Law of the Sea Conference: USSR Positions and Dilemmas," 37 pp., 10 Apr 1974, (Published in Soviet Naval Policy, Michael MccGwire; New York. Praeger) AD 783 701

PP 125

Weinland, Robert G., "Soviet Naval Operations.—Ten Years of Change," 17 pp., Aug 1974, (Published in Soviet Naval Policy, ed. Michael MccGwire; New York: Praeger) AD 783 962

PP 126 - Classified.

Dragnich, George S., "The Soviet Union's Quest for Access to Naval Facilities in Egypt Prior to the June War of 1967," 64 pp., Jul 1974, AD 786 318

Stoloff, Peter and Lockman, Robert F., "Evaluation of Naval Officer Performance," 11 pp., (Presented at the 82nd Annual Convention of the American Psychological Association, 1974) Aug 1974,

Holen, Arlene and Horowitz, Stanley, "Partial Unemployment Insurance Benefits and the Extent of Partial Unemployment," 4 pp., Aug 1974, (Published in the Journal of Human Resources, Vol. IX, No. 3, Summer 1974) AD 784 010

Dismukes, Bradford, "Roles and Missions of Soviet Naval General Purpose Forces in Wartime Pro-SSBN Operation," 20 pp , Aug 1974, AD 786 320

PP 131

Weinland, Robert G, "Analysis of Gorshkov's Navies in War and Peace," 45 pp, Aug 1974, (Published in Soviet Naval Policy, ed. Michael MccGwire; New York: Praeger) AD 786 319

Kleinman, Samuel D., "Racial Differences in Hours Worked in the Market: A Preliminary Report," 77 pp. Feb 1975, (Paper read on 26 Oct 1974 at Eastern Economic Association Convention in Albany, N Y) AD A 005 517

Squires, Michael L., "A Stochastic Model of Regime Change in Latin America," 42 pp , Feb 1975, AD A 007 912

Root, R. M. and Cunniff, P. F., "A Study of the Shock Spectrum of a Two-Degree-of-Freedom Non-linear Vibratory System," 39 pp., Dec 1975, (Pub-lished in the condensed version of The "ournal of the Acoustic Society, Vol 60, No. 6, Dec 1976, pp. 1314
*Department of Mechanical Engineering, University
of Maryland

Goudreau, Kenneth A., Kuzmack, Richard A., Wiedermann, Karen, "Analysis of Closure Alternatives for Naval Stations and Naval Air Stations," 47 pp , 3 Jun 1975 (Reprinted from "Hearing before the Subcommittee on Military Construction of the Committee on Armed Service," U.S. Senate, 93rd Congress, 1st Session, Part 2, 22 Jun 1973)

Stallings, William, "Cybernetics and Behavior Therapy," 13 pp , Jun 1975

Petersen, Charles C., "The Soviet Union and the Reopening of the Suez Canal Mineciearing Operations in the Gulf of Suez," 30 pp., Aug 1975, AD A 015 376

*CNA Professional Papers with an AD number may be obtained from the National Technical Information Service, U.S. Department of Commerce, Springfield, Virginia 27151. Other papers are available from the author at the Center for Naval Analyses, 1401 Wilson Boulevard, Arlington, Virginia 22209.

CNA Professional Papers - 1973 to Present (Continued)

PP 138
Stallings, William, "BRIDGE. An Interactive Dialogue-Generation Facility," 5 pp., Aug 1975 (Reprinted from IEEE Transactions on Systems, Man, and Cybernetics, Vol. 5, No. 3, May 1975)

N.

- PP 139 Morgan, William F., Jr., "Bayond Folklore and Fables in Forestry to Positive Economics," 14 pp., (Presented at Southern Economic Association Meetings November, 1974) Aug 1975, AD A 015 293
- PP 140
 Mahoney, Robert and Druckman, Daniel*, "Simulation, Experimentation, and Context," 36 pp., 1 Sep 1975, (Published in Simulation & Games, Vol. 6, No 3, Sep 1975)

 Refringence Inc.
- PP 141
 Mizzhi, Maurice M., "Generalized Hermite Polynomials," 5 pp, Feb 1976 (Reprinted from the Journal of Computational and Applied Mathematics, Vol 1, No. 4 (1975), 273-277).

 *Research apported by the National Science Foundation
- PP 142
 Lockman, Robert F., Jehn, Christopher, and Shughart, William F. II, "Models for Estimating Premature Losses and Recruiting District Performance," 36 pp., Dec 1975 (Presented at the RAND Conference on Defense Manpower, Feb 1976; to be published in the conference proceedings) AD A 020 443
- PP 143
 Horowitz, Stanley and Sherman, Alian (LCdr., USN),
 "Maintenance Personnel Effectiveness in the Navy,"
 33 pp. Jan 1976 (Presented at the RAND Conference
 on Defense Manpower, Feb 1976, to be published in
 the conference proceedings) AD A021 581
- PP 144

 Durch, William J., "The Navy of the Republic of China History, Problems, and Prospects," 66 pp., Aug 176 (To be published in "A Guide to Asiatic Fleets," ad. by Barry M. Blachman, Naval Institute Press) AD A030
- PP 145
 Kelly, Anne M, "Port Vints and the "Internationalist
 Mission" of the Soviet Navy," 36 pp. Apr 1976
 AD A023 436
- PP 146
 Palmour, Vernon E, "Alternatives for Increasing
 Access to Scientific Journals," 6 pp., Apr 1975
 (Presented at the 1975 IEEE Conference on Scientific
 Journals, Cherry Hill, N.C., Apr 28-30; published in
 IEEE Transactions on Professional Communication,
 Vol. PC-18, No. 3, Sep 1975) AD A021 798
- PP 147
 Kemler, J. Christian, "Legal Issues in Protecting
 Offshore Structures," 33 pp., Jun 1976 (Prepared
 under task order N00014-68-A-0091-0023 for ONR)
 AD A028 389
- PP 148
 McConnell, James M., "Military-Political Tasks of the
 Soviet Navy in War and Peace," 62 pp., Dec 1975
 (Published in Soviet Oceans Development Study of
 Senate Commerce Committee October 1976)
 AD A022 590

- PP 149 Squires, Michael L., "Counterforce Effectiveness A Comparison of the Tsipis "K" Measure and a Computer Simulation," 24 pp, Mar 1976 (Presented at the International Study Association Meetings, 27 Feb 1976) AD A022 591
- PP 150
 Kelly, Anne M. and Petersen, Charles, "Recent Changes in Soviet Naval Policy Prospects for Arms Limitations in the Mediterranean and Indian Ocean," 28 pp., Apr 1976, AD A 023 723
- PP 151
 Horowitz, Stanley A, "The Economic Consequences of Political Philosophy," 8 pp., Apr 1976 (Reprinted from Economic Inquiry, Vol. XIV, No. 1, Mar 1976)
- PP 152
 Mizrahi, Maurice M., "On Path Integral Solutions of
 the Schrodinger Equation, Without Limiting Procedure," of 10 pp. Apr 1976 (Reprinted from Journal
 of Mathematical Physics, Vol 17, No 4 (Apr 1976),
 566-575)
 **Research supported by the National Science

Foundation

- P 153
 Mizrahl, Maurice M, "WKB Expansions by Path
 Integrals, With Applications to the Anharmonic
 Oscillator," 137 pp. May 1976 (Submitted for
 publication in Annals of Physics) AD A025 440
 "Research supported by the National Science
 Foundation
- PP 154
 Mizzahi, Maurice M., "On the Semi-Classical Expansion in Quantum Mechanics for Arbitrary Hamiltonians," 19 pp., May 1976 (To appear in the Journal of Mathematical Physics) AD A025 441
- PP 155 Squires, Michael L., "Soviet Foreign Policy and Third World Nations," 26 pp. Jun 1976 (Prepared for presentation at the Midwest Political Science Association meetings, Apr 20, 1976) AD A028 388
- PP 156

 Stallings, William, "Approaches to Chinese Character
 Recognition," 12 pp., Jun 1976 (Rep-inted from
 Pattern Recognition (Pergamon Press), Vol 8, pp
 87-98, 1976) AD A028 692
- PP 157
 Morgan, William F., "Unemployment and the Pentagon Budget Is There Anything in the Empty Pork Barrel?" 20 pp., Aug 1976 AD A030 455
- PP 158
 Haskell, LCdr. Richar' D (USN), "Experimental Validation of Probability Predictions," 25 pp. Aug 1976 Presented at the Military Operations Research Society Meeting, Fall 1976) AD A030 458
- PP 159
 McConnell, James M., "The Gorshkov Articles, The New Gorshkov Book and Their Relation to Policy," 93 pp., Jul 1976 (To be printed in Soviet Navel Influence: Domestic and Foreign Dimensions, ed by M McCGwire and J McDonnell, New York. Praeger) AD A029 227
- P 160
 Wilson, Desmond P., Ir, "The U.S. Sixth Fleet and the Conventional Defense of Europe," 50 pp., Sep 1976 (Submitted for publication in Adelphi Papers, 1.1.S.S., London) AD A030 457

- PP 161
 Melich, Michael E and Peet, Vice Adm. Ray (USN, Retired), "Fleet Commanders Afloat or Ashore?" 9 pp, Aug 1976 (Repinted from U.S. Naval Institute Proceedings, Jun 1976) AD 4030 456
- PP 162
 Friedheim, Robert L, "Parliamentary Diplomacy,"
 106 pp Sep 1976 AD A033 306
- PP 163

 Lockman, Robert F, "A Model for Predicting Recruit Losses," 9 pp, Sep 1976 (Presented at the 84th annual convention of the American Psychological Association, Washington, D.C., 4 Sep 1976) AD A030 459
- PP 164

 Mahoney, Robert B., Jr., "An Assessment of Public and Elite Perceptions in France, The United Kingdom, and the Fe&ral Republic of Germany, 31 pp., Feb. 1977 (Presented at Conference "Perception of the U.S.—Soviet Balance and the Political Uses of Military Power" sponsored by Director, Advanced Research Projects Agency, April 1776) AD 036 599
- PP 165
 Jondrow, James M. "Effects of Trade Restrictions on Imports of Steel," 67 pp., November 1976, (Delivered at ILAB Conference in Dec 1976)
- PP 166
 Feldman, Paul, "Impediments to the Implementation of Desirable Changes in the Regulation of Urban Public Transportation," 2 pp. Oct 1976, AD A033 322
- PP 166 Revised Feldman, Paul, "Why it's Difficult to Change Regulation," Oct 1976
- PP 167
 Kleinman, Samuel, "ROTC Service Commitments a Comment," 4 pp., Nov 1976, (To be published in Public Choice, Vol. XXIV, Fall 1976) AD A033 305
- PP 168
 Lockman, Robert F., "Revabilition of CNA Support Personnel Selection Measures," 36 pp., Nov 1976
- PP 169

 Jacobsen, Louis S, "Earnings Losses of Workers

 Displaced from Marvifacturing Industnes," 38 pp.,

 Nov 1976, (Peliwred at ILAB Conferenc. in Dec
- PP 170
 Brechling, Frank P, "A Time Series Analysis of Labor Turnover," Nov 1976. (Delivered at ILAB Conference in Dec 1976)
- PP 171
 Raiston, James M., "A Diffusion Model for GaP Red LED Degradation," 10 pp., Nov 1976, (Published in Journal of Applied Pysics, Vol. 47, pp. 4518-4527, Oct 1976)
- PP 172
 Classen, Kathleen P., "Unemployment insurance and the Length of Unemployment," Dec 1976, (Presented at the University C. Rochester Labor Workshop on 16 Nov 1976)
- Y 173 Kleinman, Samuel D., "A Note on Racial Differences in the Added-Worker/Discouraged-Worker Controversy," 2 pp., Dec 1076, (Published in the American Economist, Vol. XX, No. 1, Spring 1976)

CNA Professional Papers - 1973 to Present (Continued)

PP 174

Malioney, Robert B., Jr., "A Comparison of the Brookings and International Incidents Projects," 12 pp Feb 1977 AD 037 206

Levine, Daniel, Stoloff, Peter and Spruill, Nancy, "Public Drug Treatment and Addict Crime," June 1976. (Published in Journal of Legal Studies, Vol. 5, No 2)

Fehr. Wendi, "Correlates of Retention and Promotion for USNA Graduates," 38 pp., Mar 1977

Lockman, Robert F and Warner, John T, "Predicting Attrition A Test of Alternative Approaches," 33 pp Mar 1977 (Presented at the OSD/ONR Conference on Enhated Attrition Xerox International Training Center, Leesburg, Virginia, 4-7 April 1977)

PP 178

Kleinman, Samuel D., "An Evaluation of Navy Unrestricted Line Officer Accession Programs," 23 pp. April 1977, (To be presented at the NATO Conference on Manpower Planning and Organization Design, Stresa, Italy, 20 June 1977;

Stoloff, Peter H and Balut, Stephen J, "Vacate A Model for Personnel Inventory Planning Under Changing Management Policy," 14 pp. April 1977, (To be presented at the NATO Conference on Manpower Planning and Organization Design, Stress, Italy, 20 June 1977)

PP 180

Horowitz, Stanley A and Sherman, Allan, "The Characteristics of Naval Personnel and Personnel Performance," 16 pp April 1977, (To be presented at the NATO Conference on Manpower Planning and Organization Design, Stress, Italy, 20 June 1977)

Balut, Stephen J and Stoloff, Peter, "An Inventory Planning Model for Navy Enlisted Personnel," 35 pp., May 1977, (Prepared for pro-itation at the Joint National Meeting of the Op-ons Research Society of America and The Institute for Management Science 9 May 1977, San Francisco, Cali-

Wheeler of the Colon Street St

Murray, Russell, 2nd, "The Quest for the Perfect Study or My First 1138 Days at CNA," 57 pp, April 1977

Kassing, David, "Changes in Soviet Naval Forces," 33 pp., November, 1976, (To be published as a chapter in a book published by The National Strategic Information Center)

PP 184

Lockman, Robert F., "An Overview of the OSD/ONR Conference on First Term Enlisted Attrition," 22 pp. June 1977, (Presented to the 29th MORS Working Group on Manpower and Personnel Planning, Annapolis, Md., 28-30 June 1977)

Kassing, David, "New Technology and Naval Forces in the South Atlantic," 22 pp (This paper was the basis for a presentation made at the Institute for Foreign Policy Analyses, Cambridge, Mass., 28 April

Mizrahi, Maurice M., "Phase Space Integrals, Without Limiting Procedure," 31 pp., May 1977, (Submitted for publication in Journal of Mathematical Physics)

Coile, Russell C, "Nomography for Operations Reenarch," 35 pp., April 1977, (Presented at the Joint National Meeting of the Operations Research Society of America and The Institute for Management Services, San Francisco, California, 9 May

PP 188

Durch, William J, "Information Processing and Outcome Forecasting for Multilateral Negotiations Testing One Approach," 53 pp., May 1977 (Pre-pared for presentation to the 18th Annual Convention of the International Studies Association, Chase-Park Plaza Hotel, St. Louis, Missoun, March 16-20, 1977)

Coile, Russell C., "Error Detection in Computerized Information Retrieval Data Bases," July, 1977, 13 pp. To be presented at the Sixth Cranfield International Conference on Mechanized Information Storage and Retneval Systems, Cranfield Institute of Technology, Cranfield, Bedford, England, 26-29 July 1977

Mahoney, Robert B., Jr., "European Perceptions and East-West Competition," 96 pp, July 1977 (Prepared for presentation at the annual meeting of the International Studies Association, St Louis, Mo . March, 1977)